

# Shower Reconstruction with the Telescope Array Fluorescence Detector



- I. *Shower Reconstruction*
- II. *Analysis in Monocular Mode*

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(Osaka City University)  
+ Telescope Array  
Collaboration



# Telescope Array Experiment



Middle Drum

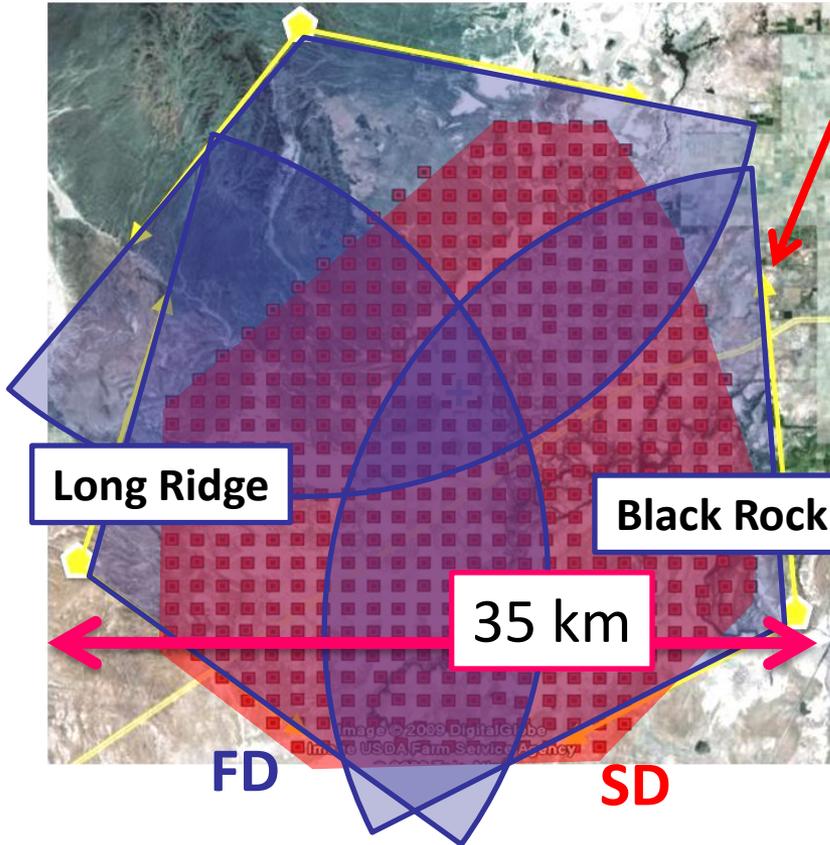


507 Surface detectors (SD)

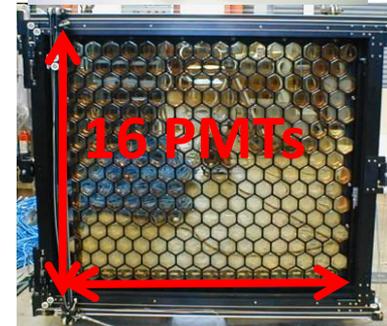
- Utah, US
- The largest detector in northern hemisphere  $\sim 700 \text{ km}^2$

## Fluorescence Detector (FD)

- Mirror Area:  $6.8 \text{ m}^2$  ( $5.2 \text{ m}^2$ )
- Camera:  $16 \times 16$  PMTs
- 12+12+14 telescopes



38 Fluorescence detector (FD)



16 PMTs

16 PMTs<sub>2</sub>



# Shower Reconstruction Procedure

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## I. PMT Selection

## II. Geometry Reconstruction

- Monocular Mode
- Stereo Mode
- Hybrid Mode

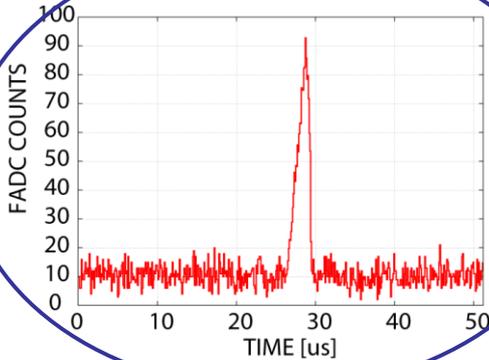
## III. Shower Profile Reconstruction

- Inverse Monte Carlo



# PMT selection

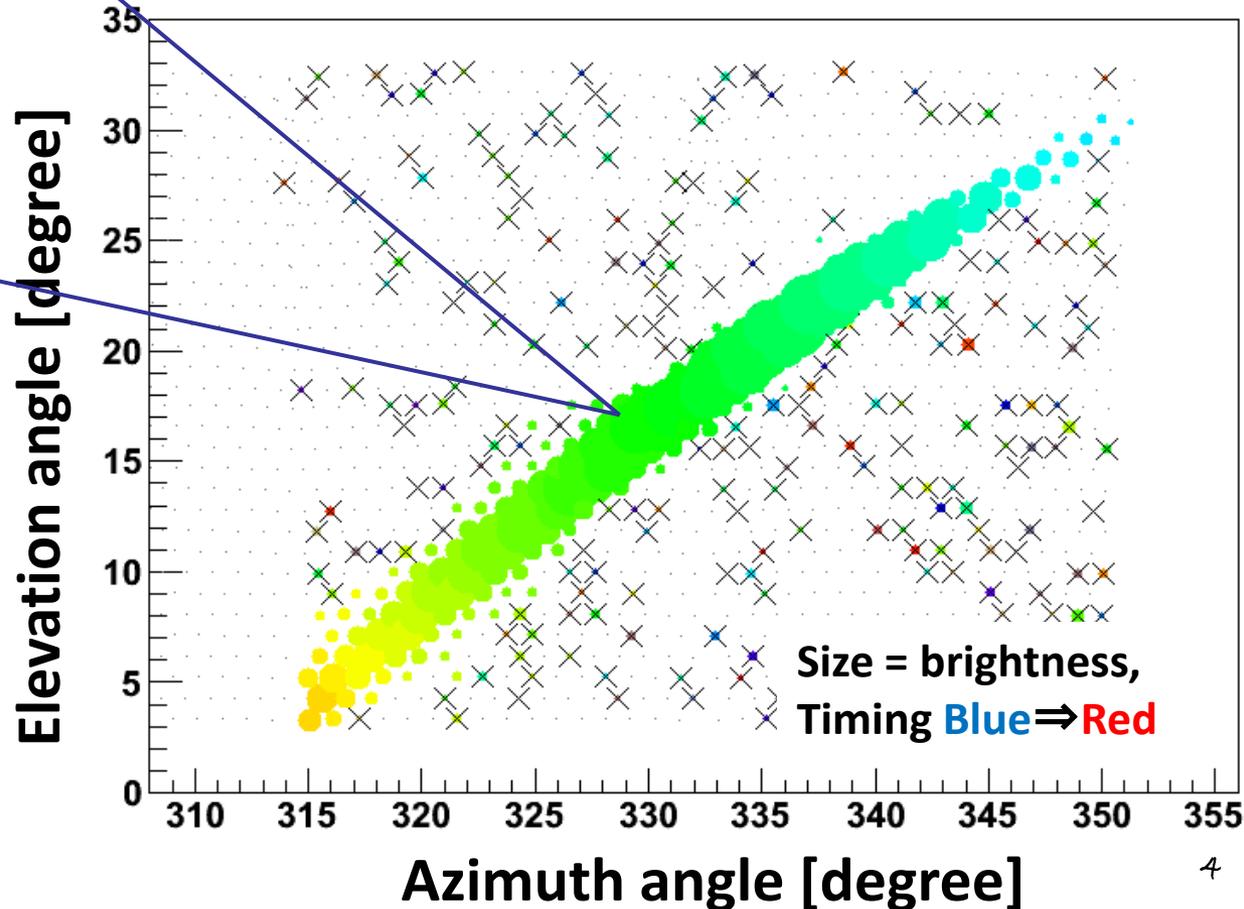
## Waveform



If include the many noise PMTs, the resolution is lower.

Air shower signal should be sequential distribution in a track and signal timing

- I. Geometrical distribution
- II. Signal timing distribution



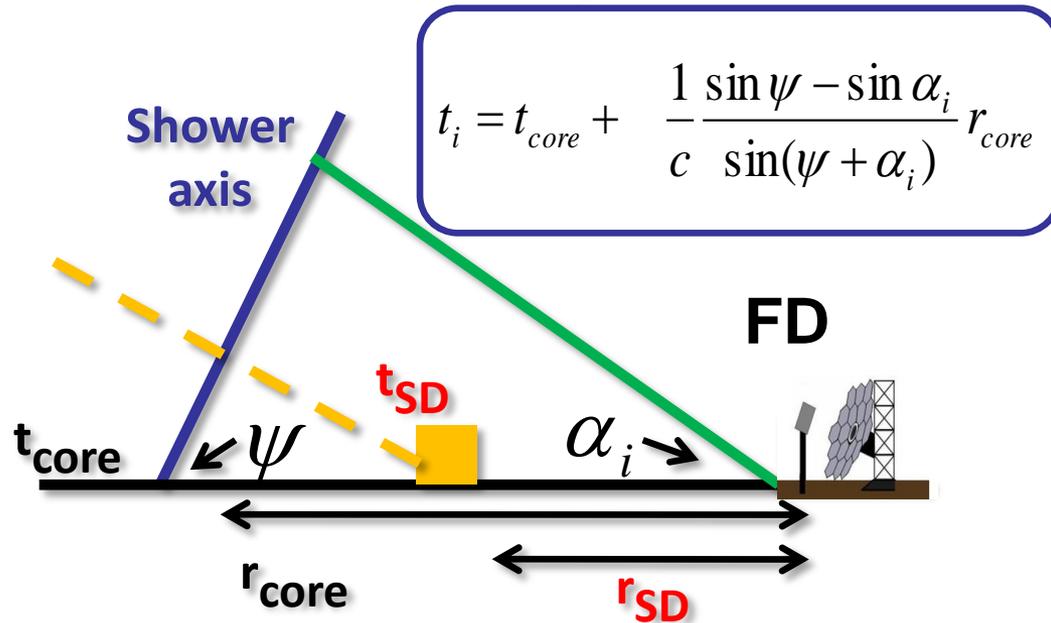


# Geometry Reconstruction

## Monocular Mode

- ◆ Only 1 FD station

Timing Fit

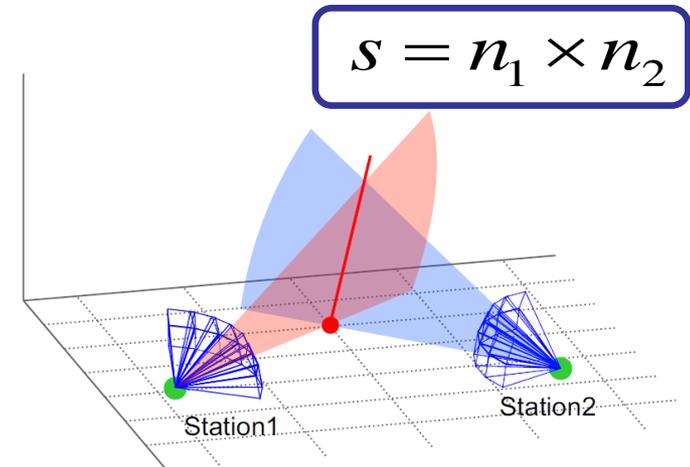


## Hybrid Mode Timing Fit by FD and SD

- ◆ FD station + SD
- ◆ Best resolution < 1°

## Stereo Mode

- ◆ 2 FD stations
- Intersection of Shower Detector Planes



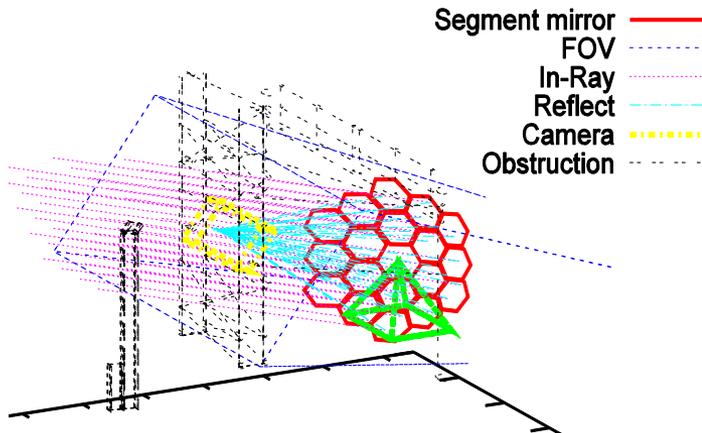
$$t_i = t_{core} + \frac{1}{c} \frac{\sin \psi - \sin \alpha_i}{\sin(\psi + \alpha_i)} r_{core}$$

$$t_{core} = \underline{t_{SD}} + \frac{1}{c} (r_{core} - \underline{r_{SD}}) \cos \psi$$



# Database of directional sensitivity

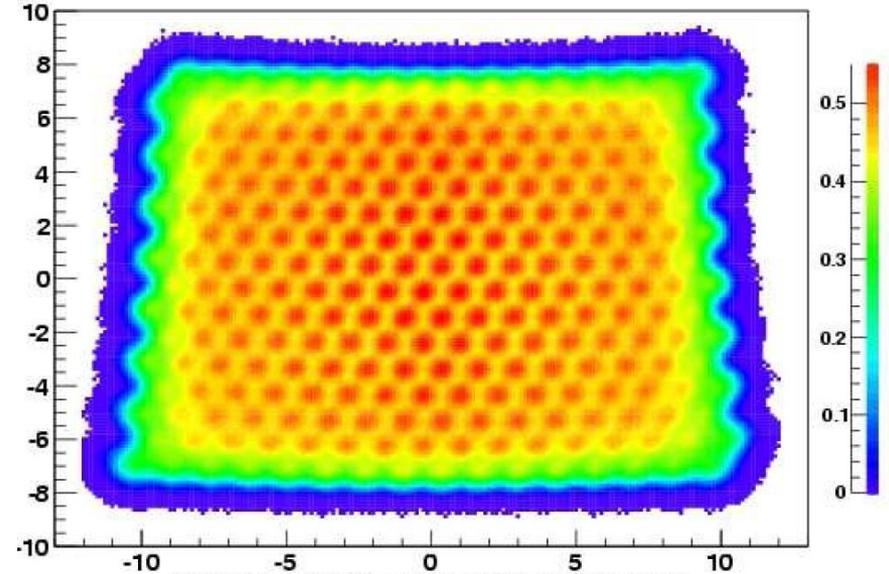
- RayTrace **parallel photons** for each direction
- Consider the following effects
  - ✓ Detector configuration and shadow
  - ✓ PMT non-uniformity (NOT depend on time)



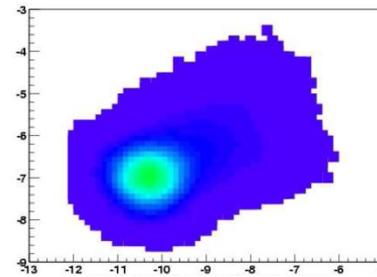
Filter transmittance and mirror reflectance = 100%

## Directional sensitivity of telescope

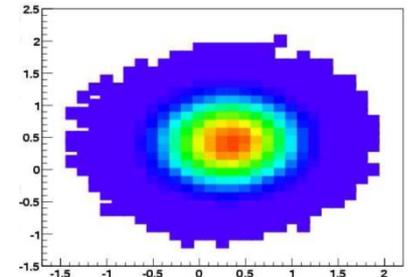
Elevation angle from telescope FOV center [deg]



Corner



Center



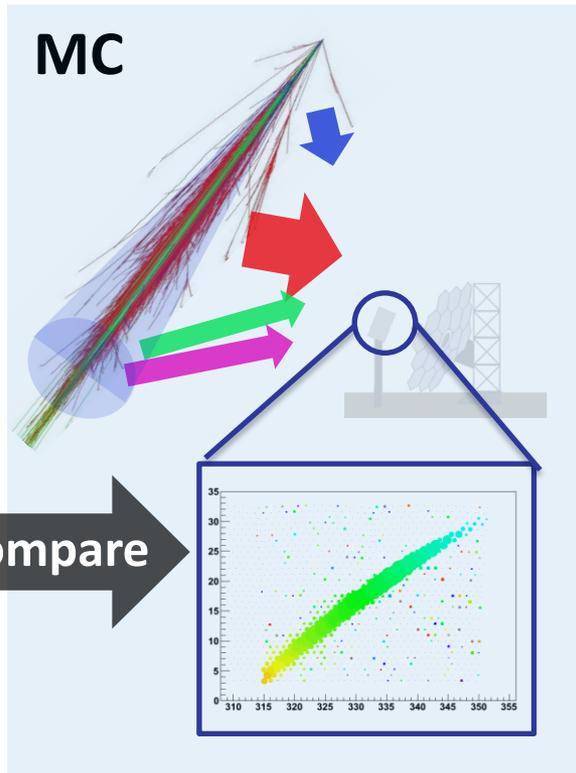
Azimuth angle from telescope FOV center [deg]



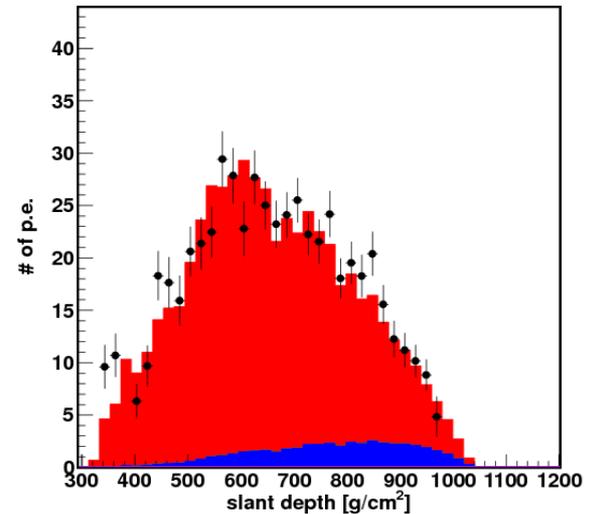
# The Concept of Inverse Monte Carlo (IMC)

Reconstructed Shower Geometry

Repeatedly calculate shower images using Database with changing longitudinal development parameters



Signal at camera



Plot: Data

Histogram(Red): Fluorescence MC

Histogram(Blue): Cherenkov MC

Size = brightness, Timing Blue  $\Rightarrow$  Red



# The detail calculation of IMC

## 1. Xmax (shower shape)

Search for the optimum Xmax in the repeated MC, maximized the following likelihood ( $X_0 = 0.0 \text{ g/cm}^2$ ,  $N_{\text{max}} = 1.0$ , fixed)

$$L = \sum_{\text{PMT}} \left\{ N_{\text{pe,data}}^{\text{PMT}} \log \left( \frac{N_{\text{pe}}^{\text{PMT}}}{N_{\text{pe}}^{\text{station}}} \right) \right\}$$

$N_{\text{pe}}^{\text{PMT}}$  : # of photo-electrons for each PMT (MC)  
 $N_{\text{pe}}^{\text{station}}$  : # of photo-electrons of station (MC)  
 $N_{\text{pe}}^{\text{station}} = \sum_{\text{PMT}} N_{\text{pe}}^{\text{PMT}}$   
 $N_{\text{pe,data}}^{\text{PMT}}$  : # of photo-electrons from Data

## 2. Nmax

$$N_{\text{pe,data}}^{\text{station}} = \sum_{\text{PMT}} N_{\text{pe,data}}^{\text{PMT}}$$

Calculate the sum of p.e. of one station for MC( $N_{\text{max}}=1.0$ ) and Data.  $N_{\text{max}}$  is a ratio between these values.

$$N_{\text{pe,Nmax=1}}^{\text{station}} = \sum_{\text{PMT}} N_{\text{pe,Nmax=1}}^{\text{PMT}}$$

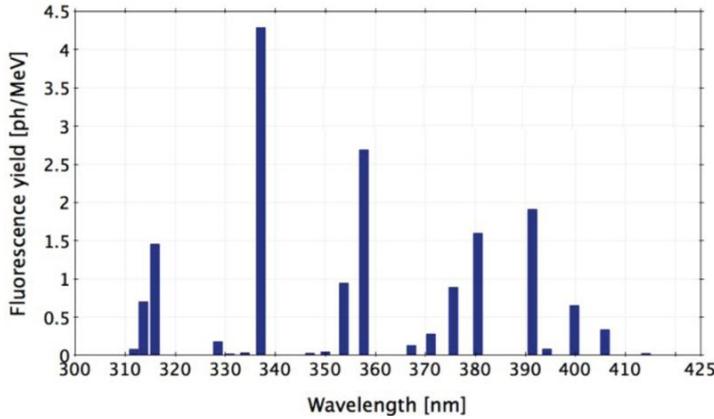
$$N_{\text{max}} = \frac{N_{\text{pe,data}}^{\text{station}}}{N_{\text{pe,Nmax=1}}^{\text{station}}}$$

## 3. Energy

Integrate energy deposit and correct invisible energy  $E_{\text{cal}} = \left\langle \frac{dE}{dX} \right\rangle \int_X N(X : X_{\text{max}}, N_{\text{max}}, X_0) dX$



# Energy Systematic Uncertainty (Hybrid Mode)



**Fluorescence Yield** **11%**

Spectrum: FLASH

*Abbassi et al., Astropart. Phys., 29 77-86 (2008)*

Absolute: Kakimoto *et al.*

*Kakimoto et al., NIM A, 372 527-533 (1996)*

Source	$\Delta E / E$
Fluorescence yield	11%
Calibration	10%
Atmosphere	11%
Reconstruction	10%
<b>Total</b>	<b>21%</b>



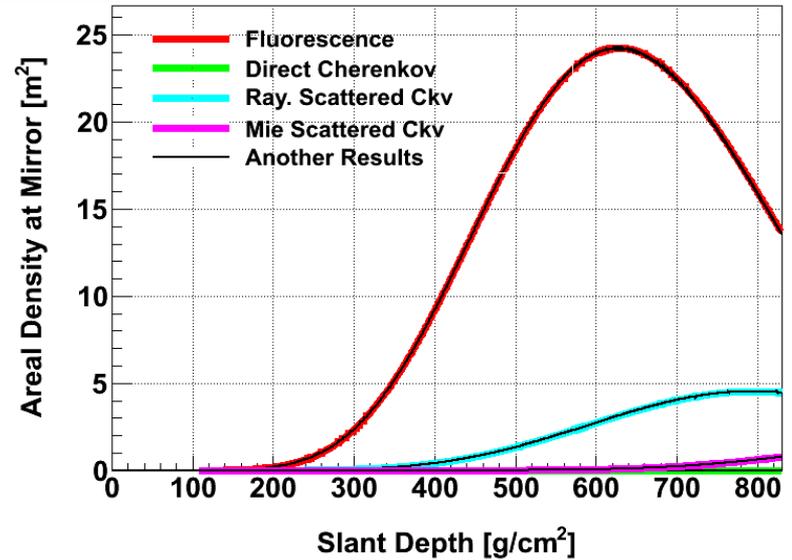
# Cross check with another software

Compare with another independently developed software

## Cross Check 1

◆ Generate the perfectly identified air shower in both simulations

**Photon density at mirror is completely agreement**

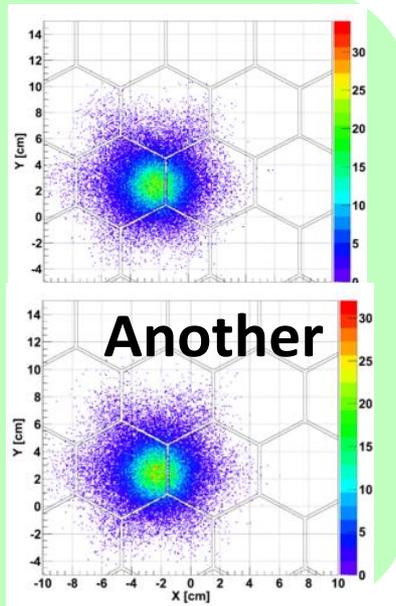


## Cross Check 2

Raytrace from Point source

- Detector configuration
- Detector Shadow

**Good agreement < 2%**



## Cross Check 3

data analysis independently

- PMT selection
- Geometry reconstruction
- Shower profile reconstruction

**Reconstructed Energy is good agreement < 4%**



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# FD Analysis in Monocular Mode

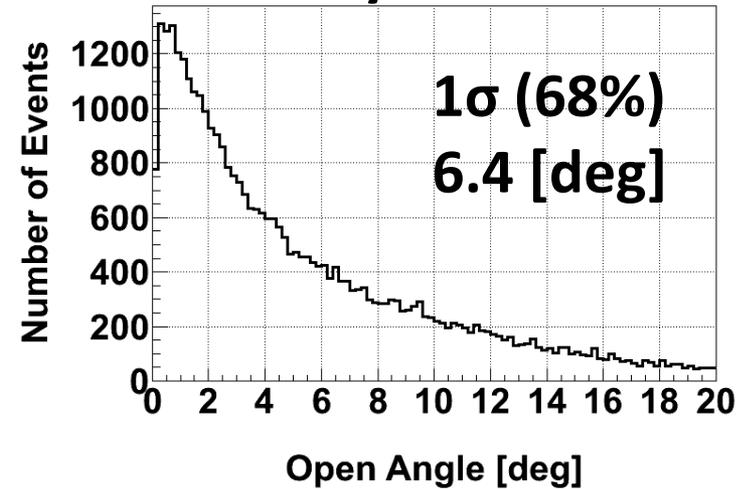


# MC study: Resolution in Monocular Mode

## Monocular analysis

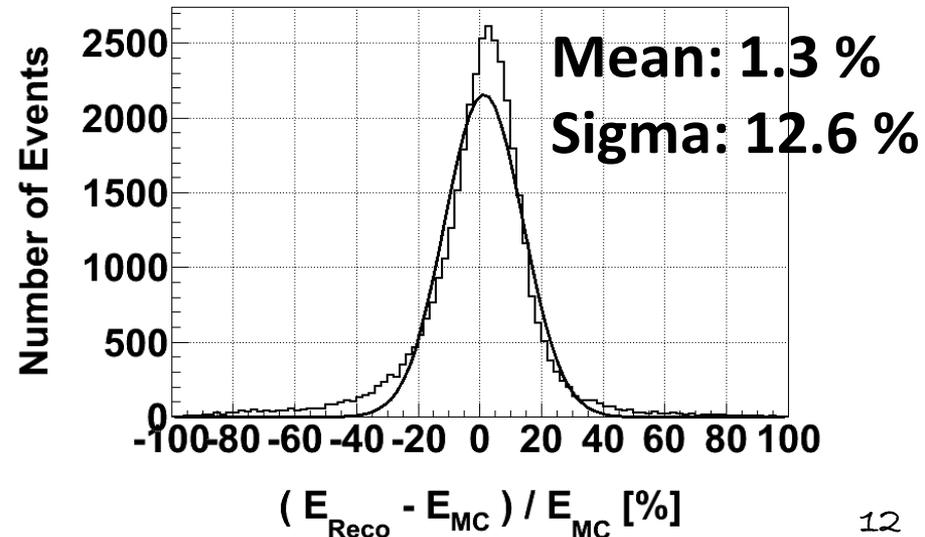
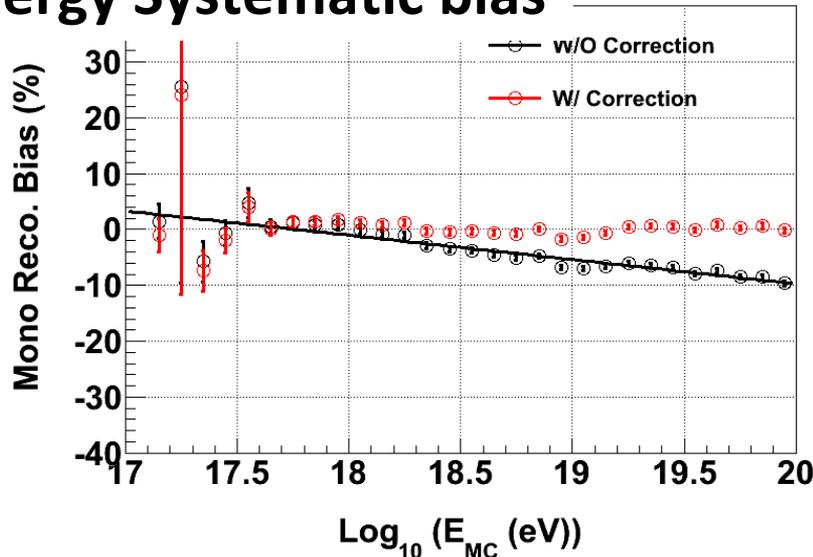
- ◆ Corsika QGSJET-II **Proton**
- ◆ LogE: 17.0 - 20.0
- ◆ Spectrum index = -1.0
- ◆ Zen: 0-65 deg, Azi: 0-360 deg
- ◆ Core: less than 35 km from TA Center

## Geometry Resolution



## Energy Resolution

### Energy Systematic bias



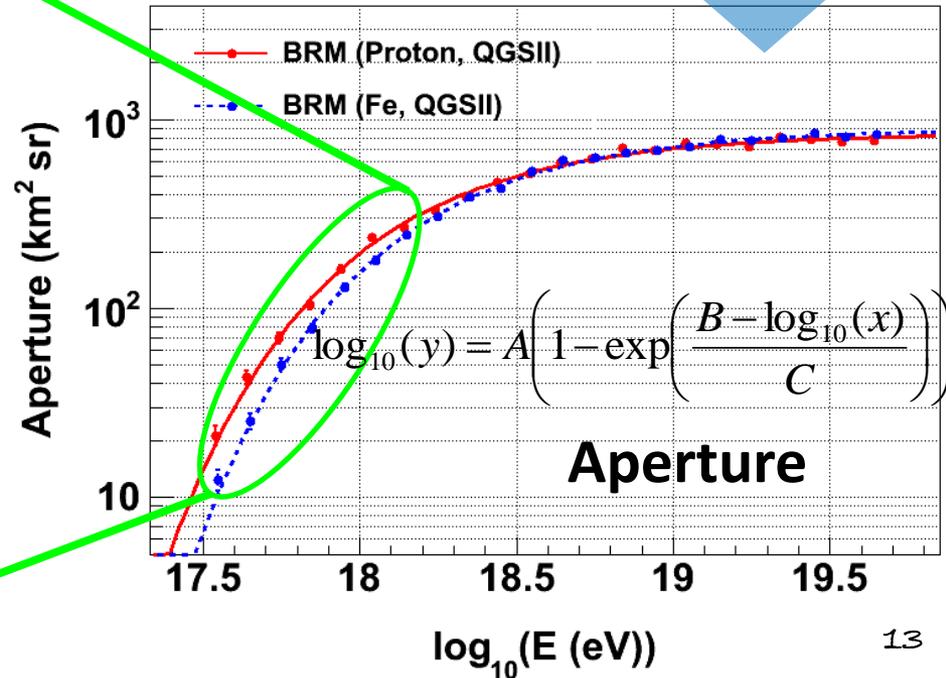
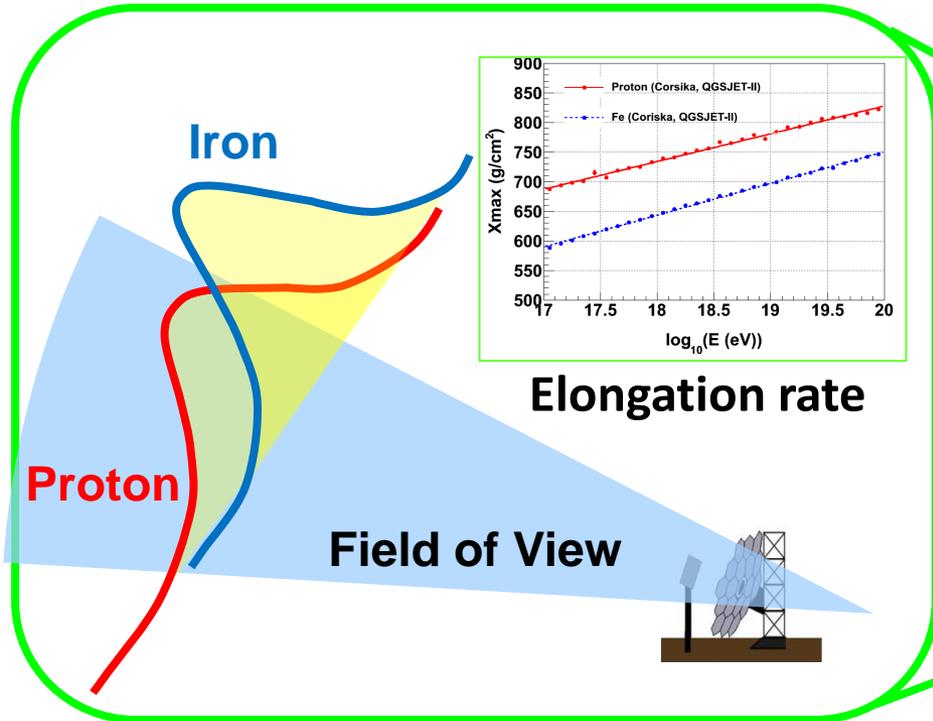
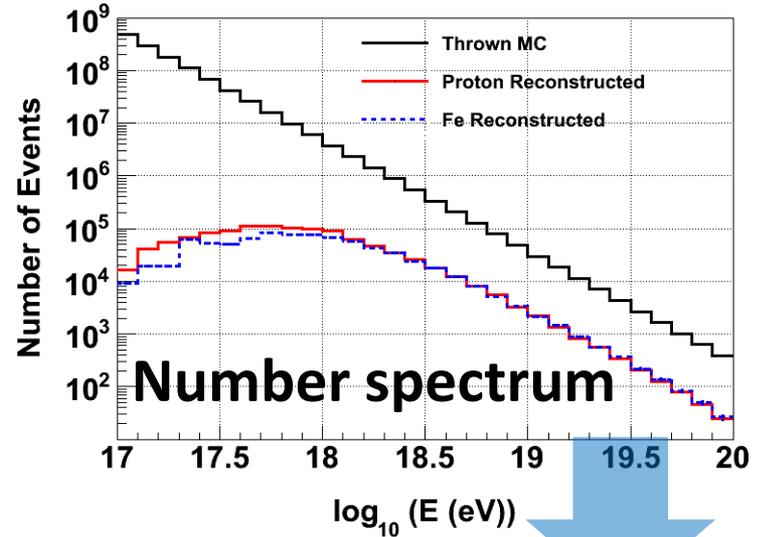
# Aperture calculation in Monocular Mode

Model: Corsika (QGSJET-II)

Proton and Iron

$$Aperture = Area^{MC} \times \frac{\#reco.}{\#MC}$$

Weight:  $J(E) \propto E^{-3.1}$



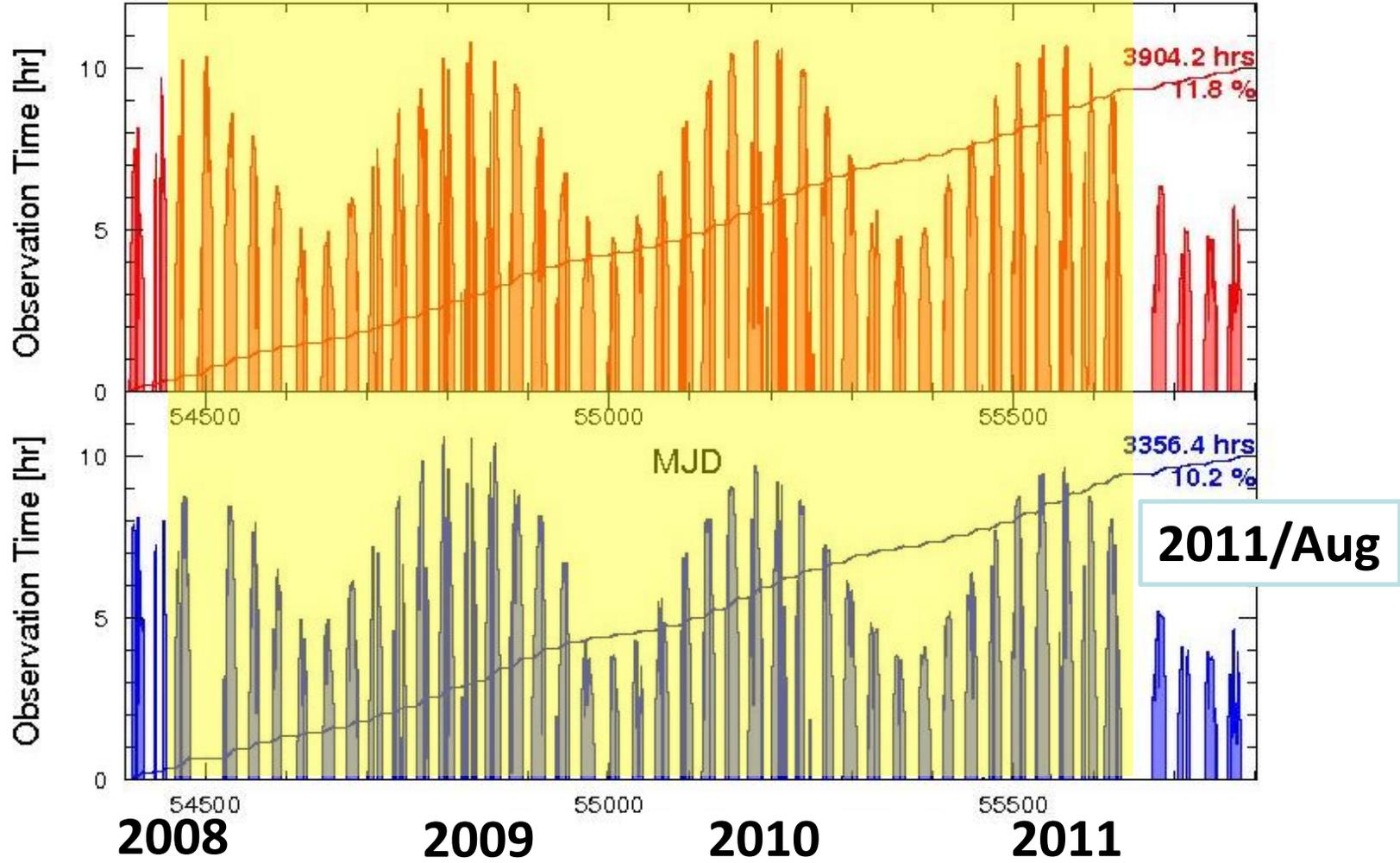


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# Data Analysis in Monocular Mode



# Observation Time and Data Set

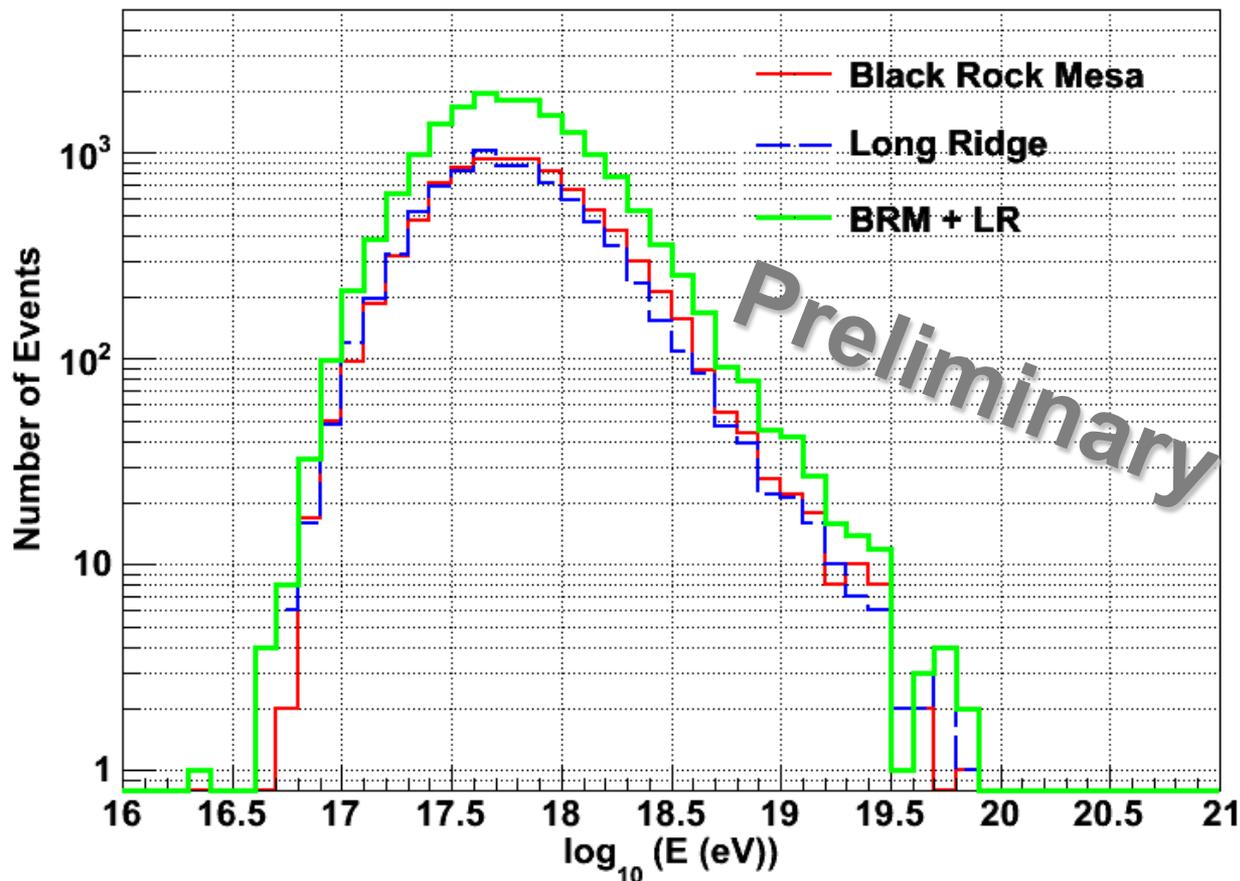


**2008/Jan/01 ~ 2011/Mar/13 3.3 yrs (Monocular analysis)**

**BRM: 2280 hrs LR: 1974 hrs (cloud cut and dead time subtracted)**



# Number Spectrum (Data)



**Black Rock Mesa: 8905 events**, **Long Ridge 8378 events**,  
**BRM+LR 17208 events**

(selected the result with a larger number of photo-electrons)

**1 station: 1 air shower for every 15 min.**



# Data/MC comparison

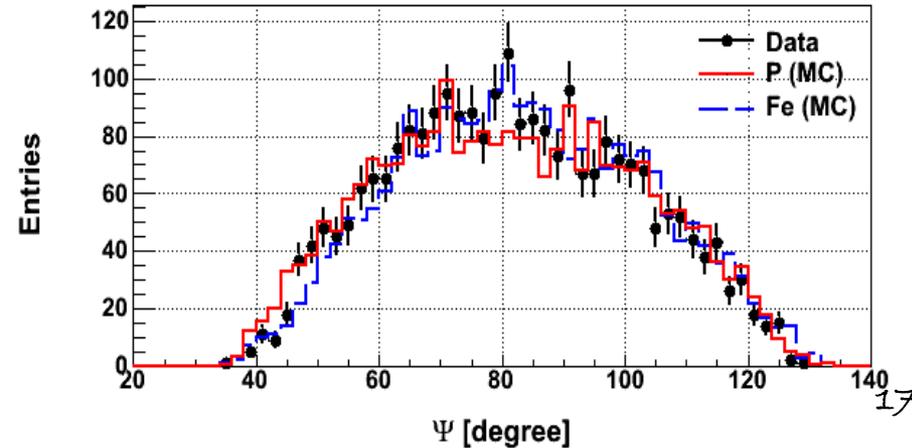
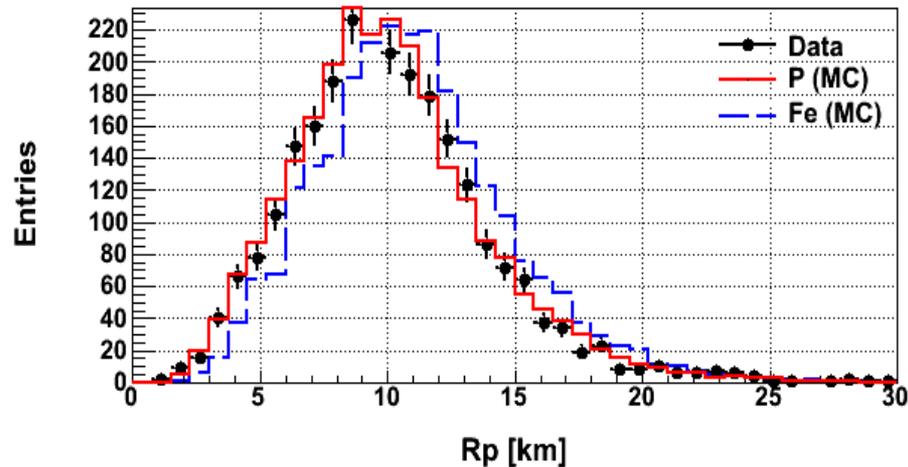
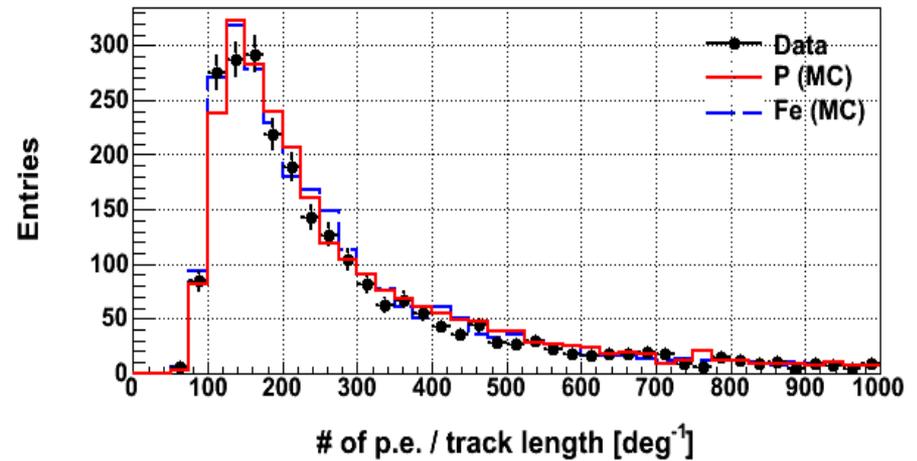
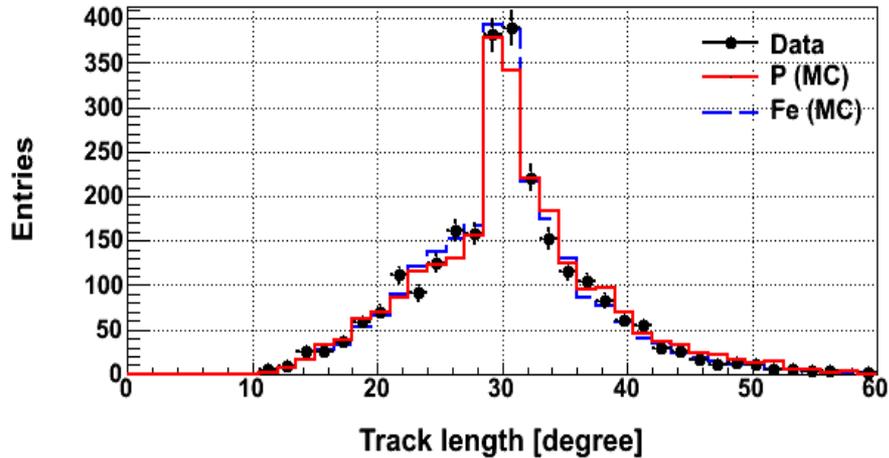
## Black Rock Mesa

Energy >  $10^{18}$ eV

Histogram(Red): Proton MC

Histogram(Blue): Fe MC

Plot: Data





# Summary

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- FD analysis in Monocular Mode
  - Resolution:
    - Arrival direction 6.4 [deg]
    - Energy: 12.6%
- Good agreement for cross check with another independently developed software
- BRM and LR data analysis during 3.3 yrs in Monocular Mode
- Data/MC comparison is very consistent

## Future plans

- Energy spectrum, mass composition