



# Measurement of the single top t-channel cross section at CMS

GK Workshop Bad Liebenzell 2012

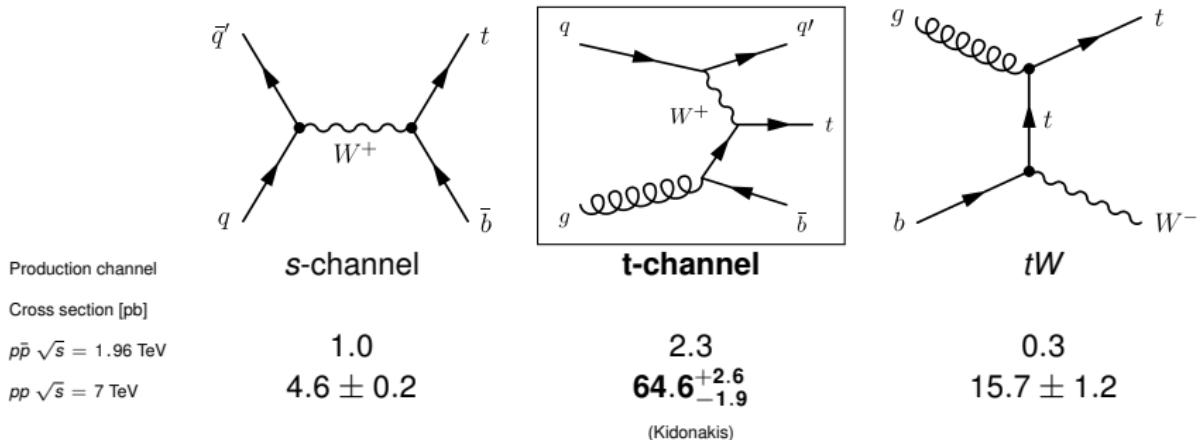
Steffen Röcker | 10.10.2012

INSTITUT FÜR EXPERIMENTELLE KERNPHYSIK



rahul rekapalli  
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# Single top production

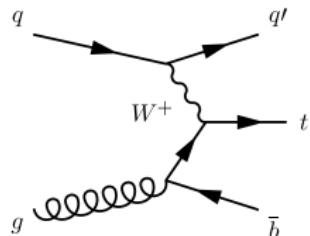


- Virtuality of the involved  $W$  boson  $\rightarrow$  three different production mechanisms
- $t$ -channel and  $tW$  cross sections largely enhanced at LHC due to gluon splitting
- $t$ -channel and  $tW$  depend on b-quark PDF (up to 4%  $\Delta\sigma$ )
- Largest cross section at Tevatron and LHC:  $t$ -channel

# Single top - history and motivation

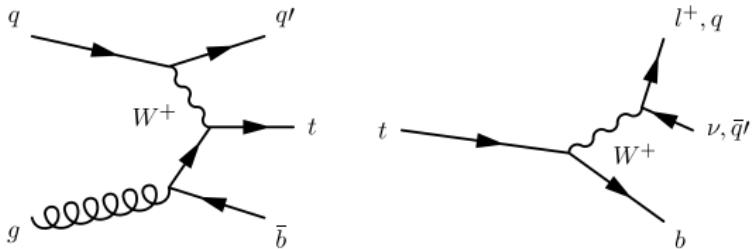
- Single top quark production first discovered in 2009 at Tevatron by CDF and DØ
- Discovery in  $s+t$ -channel after long and difficult search
- Rediscovery of  $t$ -channel in 2011 at LHC with first data
- Can now be studied in detail at LHC

Interesting properties:

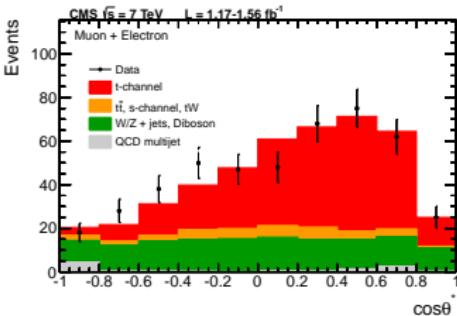


- Allows direct measurement of CKM matrix element  $|V_{tb}|$
- Sensitive to  $b$  quark PDF
- $Wtb$  coupling enables tests of V–A structure, anomalous couplings
- Allows study of top quark polarization
- Background for Higgs/SUSY and search for new physics (4th generation,  $H^+$ ,  $W'$ )

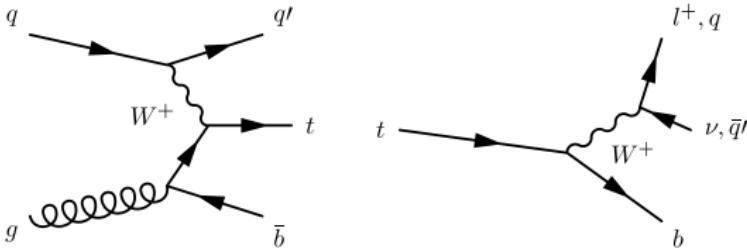
# Top quark decay



- Top quark decays immediately due to high mass / large width
- Top quark decays into  $W$  boson and  $b$  quark (SM: BR  $\approx 100\%$ )
- $W$  boson from top-quark decay further decays into charged lepton and neutrino (BR  $\approx 32\%$ ), here only muon and electron channel
- Spin information passed to decay products



# Event selection

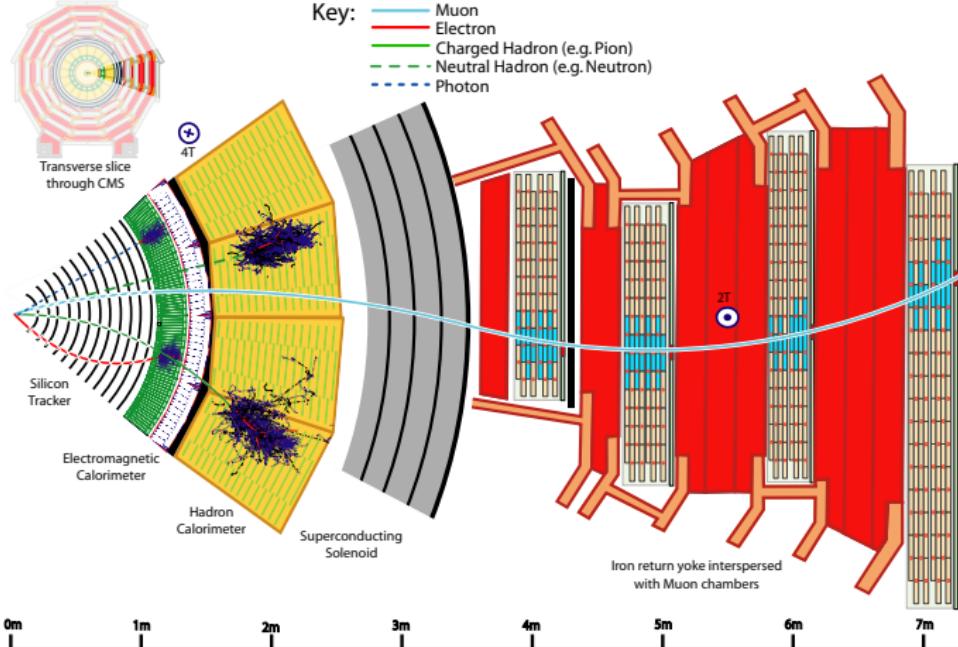


- Muon (electron+b-jet) trigger → data set 1.17/fb (1.56/fb)
- 1 isolated muon (electron) with  $p_T > 20(30)$  GeV/c and  $|\eta| < 2.1$  (2.5)
- Veto electrons (muons) and loose muons (electrons)  
in muon (electron) decay channel
- $MTW > 50$  GeV/c $^2$  ( $E_T^{miss} > 35$  GeV/c $^2$ ) to suppress QCD



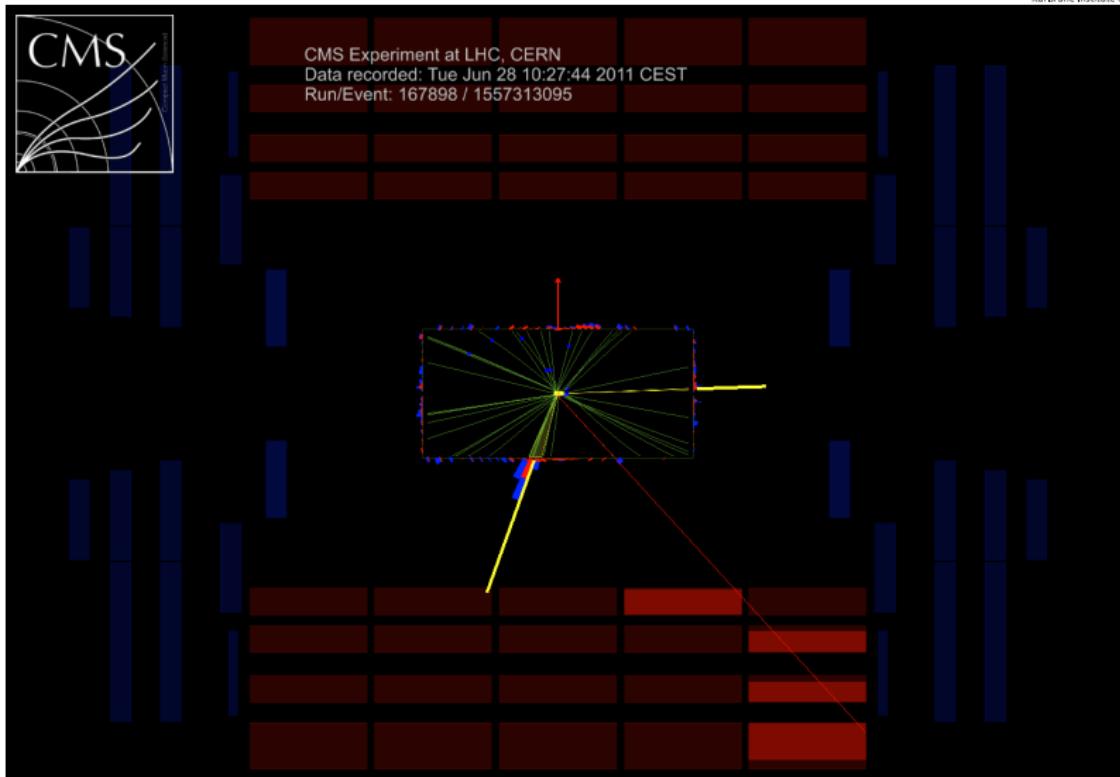
- 2,3 or 4 jets with  $p_T > 30$  GeV/c and  $|\eta| < 4.5$
- 0, 1 or  $\geq 2$  jets with b-tag (0.1% mistag rate)

# CMS detector

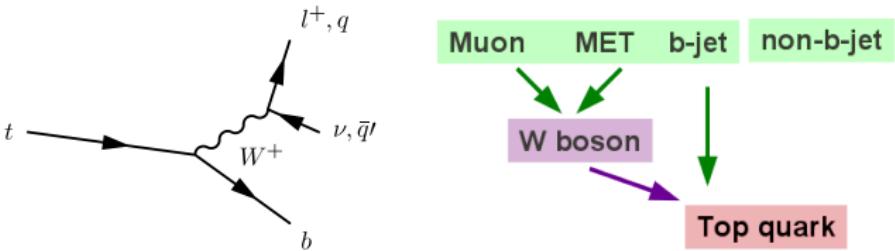


- Single top analyses need information from all detector subsystems to reconstruct (forward) jets, leptons, and missing transverse energy ( $E_T^{\text{miss}}$ )

# Event Display - $\rho$ – z plane



# Top quark reconstruction

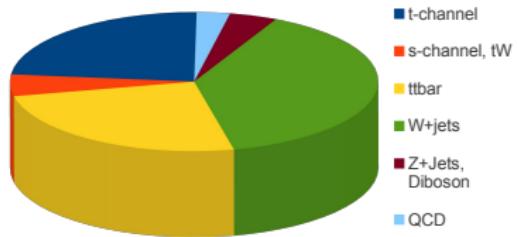


- Reconstructed from detector: jets, leptons,  $E_T^{miss}$
- Top quark candidate reconstructed from  $W$  boson and  $b$ -tagged jet
- $W$  boson from lepton and  $E_T^{miss}$ :  $p_{z,\nu}$  from  $E_T^{miss}$  by constraint on  $W$  boson mass
  - Two real solutions: Choose the one with smallest  $|p_{z,\nu}|$
  - Imaginary solution: Minimal variation of  $E_T^{miss}$  so that  $M_T^W = M_W$
- Assign  $b$ -tagged jet to top quark decay
  - Assignment of top quark correct in approx. 88% of cases (MC studies)

# Backgrounds

- Contribution from background processes after selection:

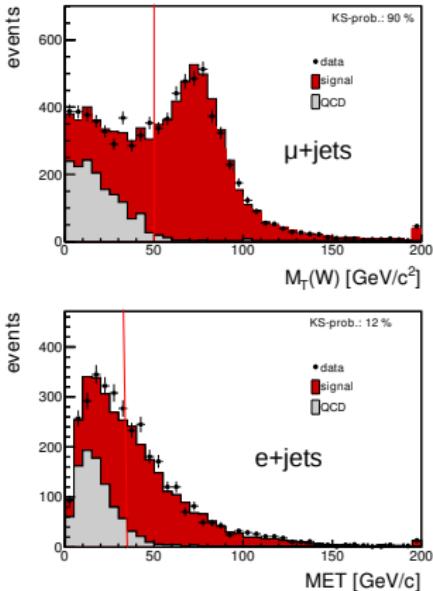
- Single Top:  $s$ -channel,  $tW$
- $W$ +jets
- Top quark pair production  $t\bar{t}$
- $Z$ +jets
- Diboson ( $WW$ ,  $WZ$ ,  $ZZ$ )
- QCD multijet



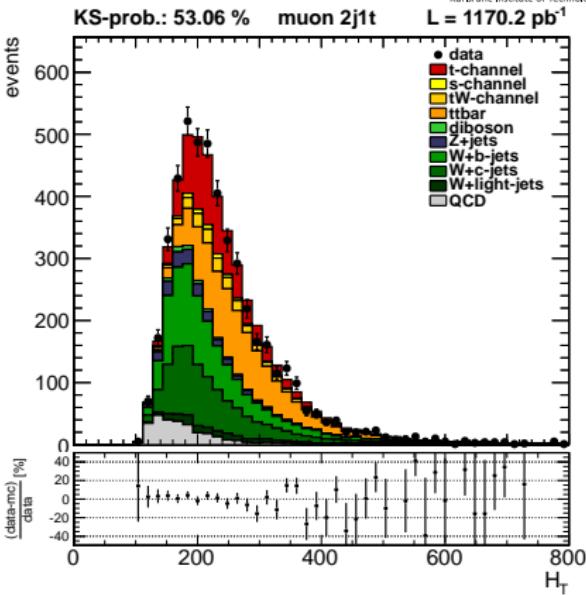
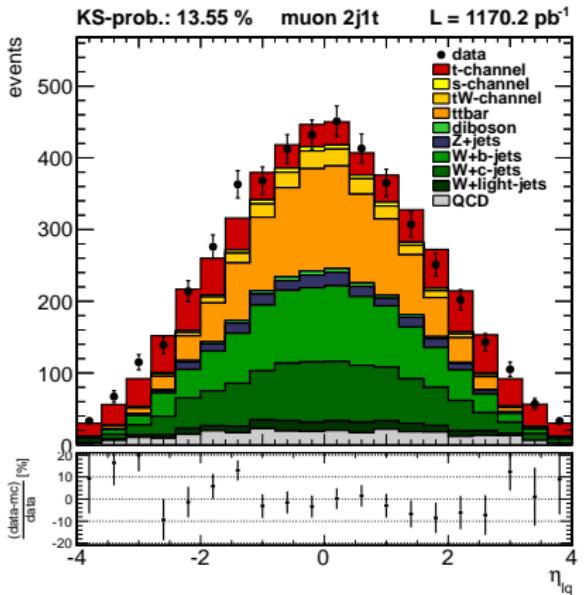
- Main backgrounds:  $W$ +jets and top quark pair production  $t\bar{t}$
- QCD multijet background difficult to model,  
MC statistics very small → data driven estimation

# Data driven background estimation

- QCD multijet distribution extracted from orthogonal data set:
- Muon channel:
  - Invert relative isolation cut
- Electron channel:
  - Anti-Electron ID  
(2 out of 3 criteria must not be fulfilled )
- Orthogonal selection has been checked in MC
- Fit to transverse mass of W boson ( $M_{T\bar{W}}$ ) /  $E_T^{\text{miss}}$  before cut to extract shape and rate
- $F(x) = a \cdot S(x) + b \cdot B(x)$



# Discriminating variables

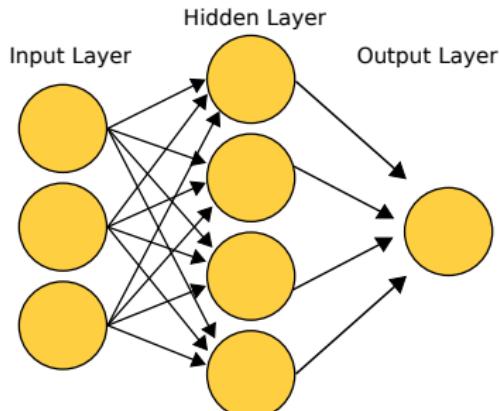


- Pseudorapidity of light quark mostly in forward region
- Other variables alone: not much separation power
- → Use a multivariate technique

- Artificial neural networks (NN) modeled after biological neural networks
- Multiple nodes with nonlinear activation function in three or more layers, each node connected to every node in the next layer with specific weight
- The network learns by minimizing an error function and changing the weights (Supervised learning, backpropagation)

## NeuroBayes:

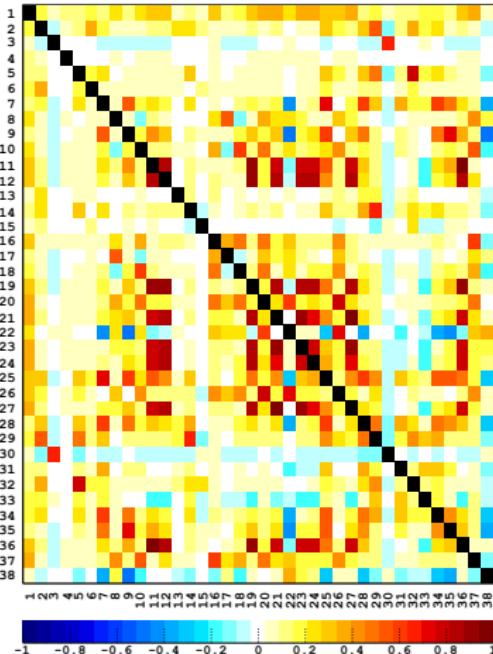
- 3-layer feedforward network
- Robust preprocessing of input variables (Decorrelation, transformation to Gaussian)
- Spline-fit to variables to be robust against statistical fluctuations or noise



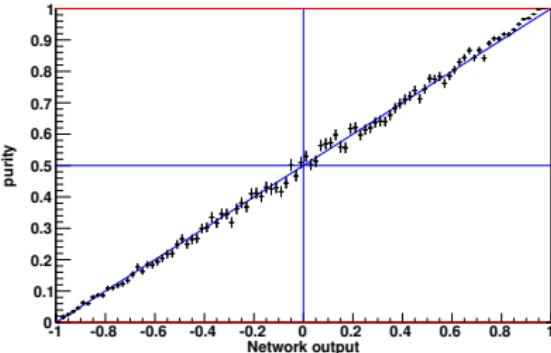
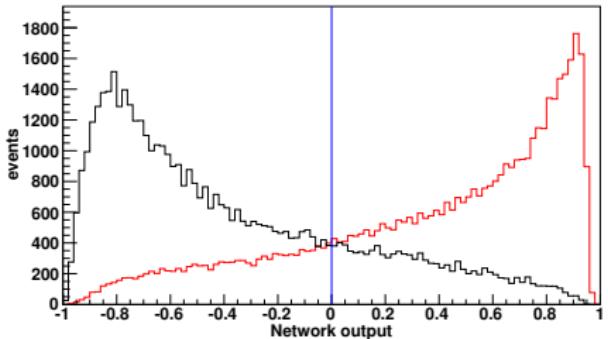
# Neural network - input variables

- Detailed studies of multiple variables
- Only use well modeled variables,  
i.e. those with good KS test values in  
control region
- Network rejects variables with low  
significance
- 37 variables in muon channel  
38 variables in electron channel
- Most important variables: light quark  $\eta$ ,  
 $H_T$ ,  $M_{jet1,jet2}$

correlation matrix of input variables

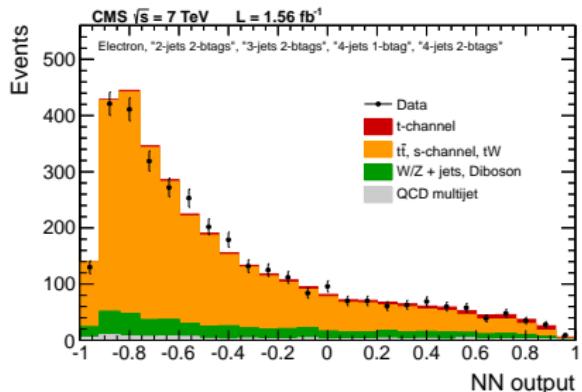
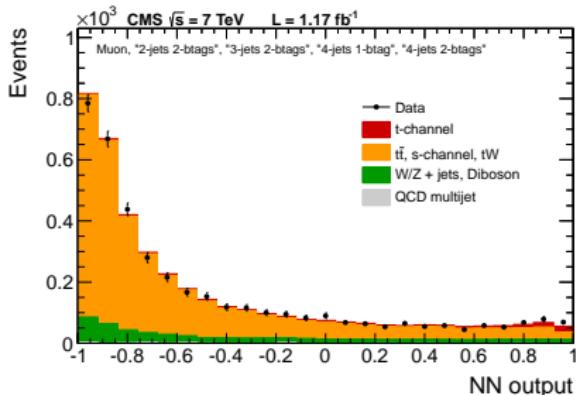


# Neural network - training



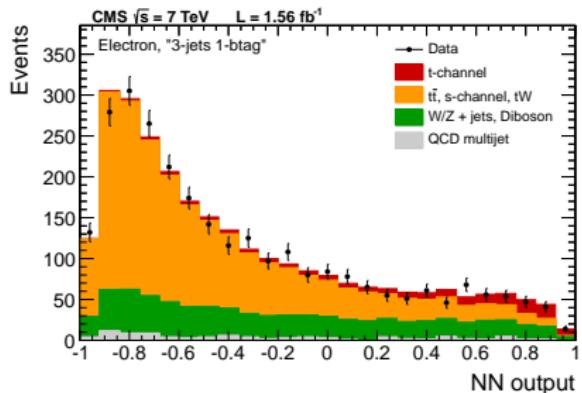
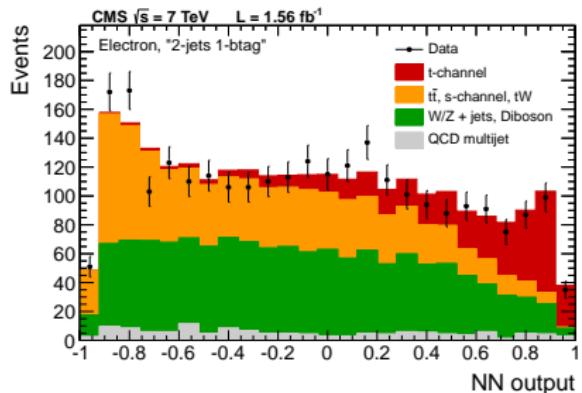
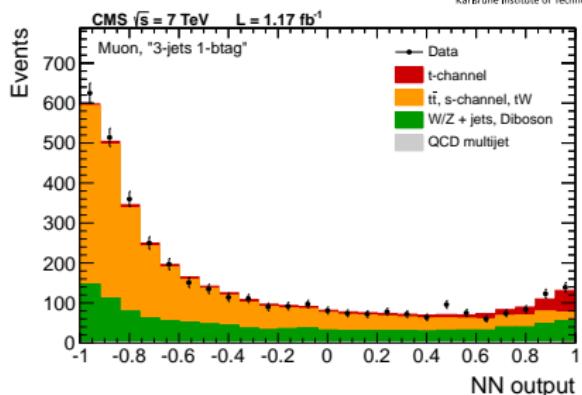
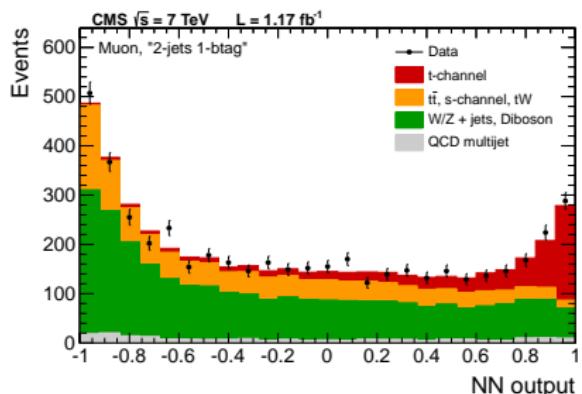
- Signal/background ratio 50:50 ( $t$ -channel vs  $t\bar{t}$ ,  $W$ +jets,  $Z$ +jets)
- Network can separate **signal** and **background**
- Purity increases with discriminator output

# Neural network - discriminator in background region



- Discriminator output well modeled in  $t\bar{t}$  enriched background region

# Neural network - discriminator in signal region



# Statistical inference

- Bayesian method

$$p(\mu | \text{data}) \propto \int p'(\text{data} | \mu, \vec{\theta}) \cdot \pi(\mu) \pi(\vec{\theta}) d\vec{\theta}$$

- Impact of systematic effects marginalized as nuisance parameters (JER, JES, b-tagging, ...)
- Influence of theoretical uncertainties studied separately, not marginalized (Renormalization/factorization ( $Q^2$  scale), matching, PDF, different signal generator)
- Integration via Markov Chain Monte Carlo (MCMC)
- Statistical framework: <http://www.theta-framework.org>
- Cross section for electrons, muons:

$$\sigma_{t\text{-ch.}} = 69.7^{+7.2}_{-7.0} \text{ (stat. + syst. + lum.)} \pm 3.6 \text{ (theor.) pb} \quad (\text{muons})$$

$$\sigma_{t\text{-ch.}} = 65.1^{+9.2}_{-8.9} \text{ (stat. + syst. + lum.)} \pm 3.5 \text{ (theor.) pb} \quad (\text{electrons})$$

- and combined:

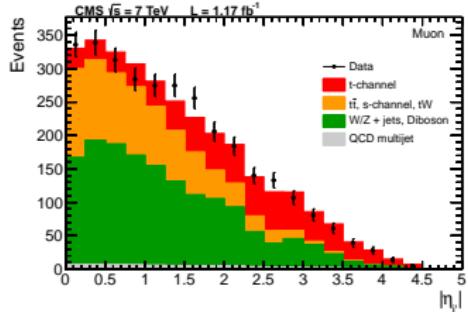
$$\sigma_{t\text{-ch.}} = 68.1 \pm 4.1 \text{ (stat.)} \pm 3.4 \text{ (syst.)}^{+3.3}_{-4.3} \text{ (theor.)} \pm 1.5 \text{ (lum.) pb}$$

# Combination

This measurement is combined with two other measurements:

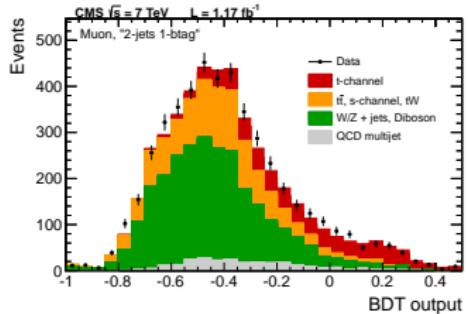
- Light quark  $\eta$  analysis (Napoli)

- Template fit to light quark  $\eta$
- $W+jets$  background data driven
- One analysis bin (2 jets 1 tag)



- BDT analysis (Aachen)

- MVA analysis (BDT)
  - Bayesian method
  - Multiple analysis bins
- } same as NN



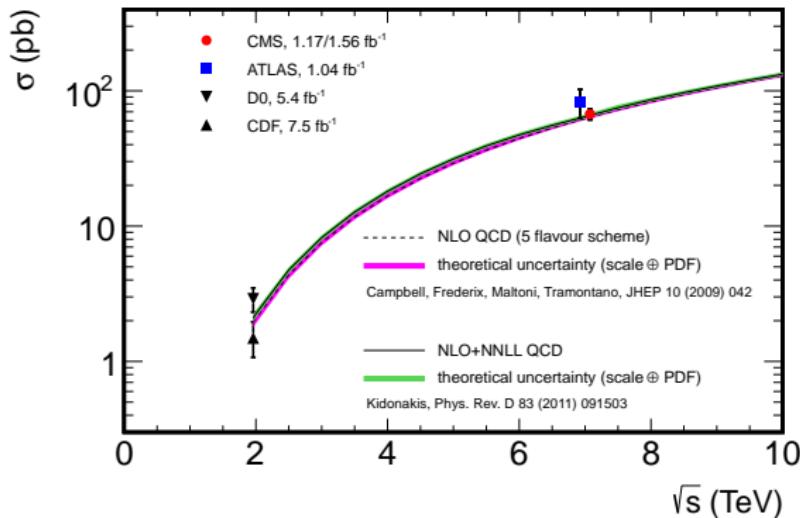
- All three analyses employ the same selection
- Correlation is estimated by dicing toys

# Combination - Result

- Combining all three analyses with BLUE yields a cross section of

$$\sigma_{t\text{-ch.}} = \boxed{67.2 \pm 6.1 \text{ pb}} = 67.2 \pm 3.7 \text{ (stat.)} \pm 3.0 \text{ (syst.)} \pm 3.5 \text{ (theor.)} \pm 1.5 \text{ (lum.) pb}$$

- with a relative uncertainty of 9.1%
- Published in TOP-011-021 (arXiv:1209.4533), submitted to JHEP



# Combination - Estimation of $|V_{tb}|$

- Under the assumption that  $|V_{tb}|^2 \gg |V_{td}|^2 + |V_{ts}|^2$  and  $|V_{tb}| = 1$  for  $\sigma_{t\text{-ch.}}^{\text{th}}$ .
- One can extract  $|V_{tb}|$  from the cross section measurement

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

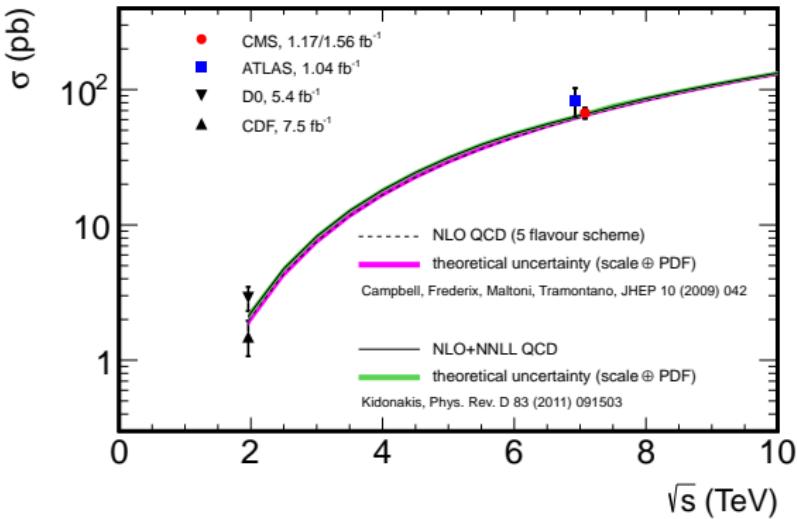
$$|f_{LV} V_{tb}| = \sqrt{\frac{\sigma_{t\text{-ch.}}}{\sigma_{t\text{-ch.}}^{\text{th}}}} = 1.020 \pm 0.046 \text{ (exp.)} \pm 0.017 \text{ (theor.)}$$

- with a possible anomalous form factor  $f_L$  from BSM models
- Constraining  $|V_{tb}|$  to the interval  $[0, 1]$  and setting  $f_L = 1$  yields: (Feldman Cousins)

$$0.92 < |V_{tb}| \leq 1 @ 95\% \text{ CL}$$

# Conclusion

- Measured single top t-channel cross section and  $|V_{tb}|$  with neural network analysis in multiple channels at  $\sqrt{s} = 7$  TeV
- Combination yields cross section with relative uncertainty  $< 10\%$
- Most precise single top  $t$ -channel cross section measurement
- $|V_{tb}| \approx 1$  and  $0.92 < |V_{tb}| \leq 1$  @ 95% CL



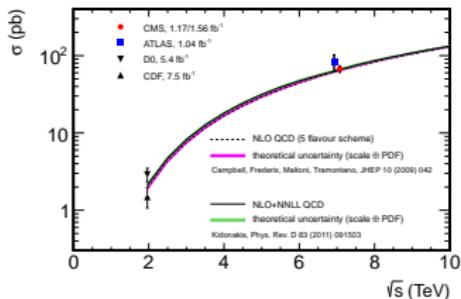
# Conclusion and outlook

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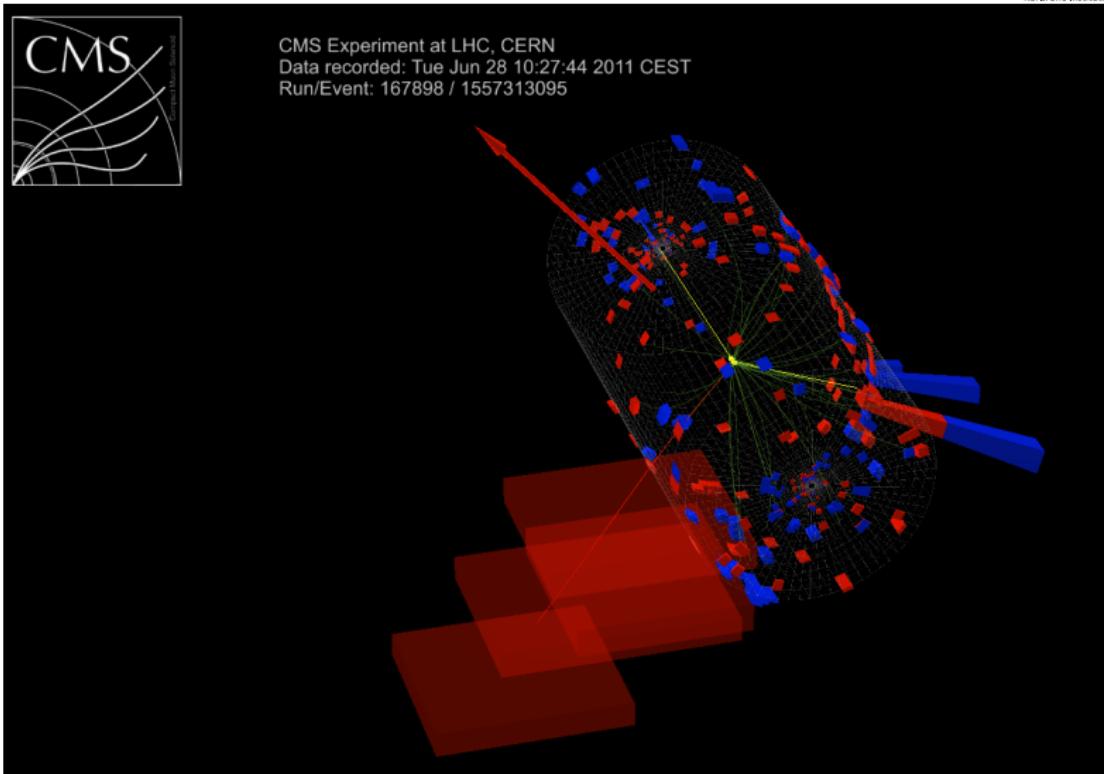
Outlook:

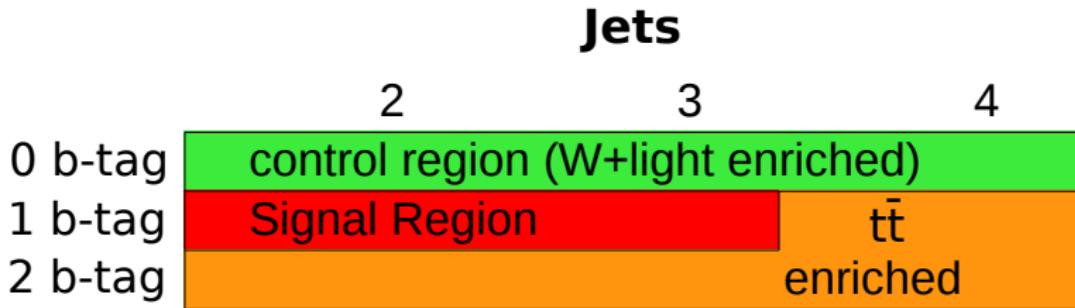
- Already recorded  $15/\text{fb}$  at  $\sqrt{s} = 8 \text{ TeV}$  this year
- Detailed studies of theory possible:
  - Differential measurement in top  $p_T$  and  $\eta$
  - Polarization of top quarks
  - ...



# Backup

# Event Display - 3D view





- Events without  $b$ -tag:  
(W+light enriched) control region of input variables
- Events with  $\geq 2$   $b$ -tags:  
Estimation of top quark pair production and constraint of systematic effects

# Systematic effects

Table: Sources of uncertainty on the cross section measurement.

		Uncertainty source	NN	BDT	$\eta_{J/\psi}$
Marginalised (NN, BDT)	Experimental uncert.	Statistical	-6.1/+5.5%	-4.7/+5.4%	$\pm 8.5\%$
		Limited MC data	-1.7/+2.3%	$\pm 3.1\%$	$\pm 0.9\%$
		Jet energy scale	-0.3/+1.9%	$\pm 0.6\%$	-3.9/+4.1%
		Jet energy resolution	-0.3/+0.6%	$\pm 0.1\%$	-0.7/+1.2%
		b tagging	-2.7/+3.1%	$\pm 1.6\%$	$\pm 3.1\%$
		Muon trigger + reco.	-2.2/+2.3%	$\pm 1.9\%$	-1.5/+1.7%
		Electron trigger + reco.	-0.6/+0.7%	$\pm 1.2\%$	-0.8/+0.9%
		Hadronic trigger	-1.3/+1.2%	$\pm 1.5\%$	$\pm 3.0\%$
		Pileup	-1.0/+0.9%	$\pm 0.4\%$	-0.3/+0.2%
		MET modeling	-0.0/+0.2%	$\pm 0.2\%$	$\pm 0.5\%$
Backg. rates	Backg. rates	W+jets	-2.0/+3.0%	-3.5/+2.5%	$\pm 5.9\%$
		light flavor (u, d, s, g)	-0.2/+0.3%	$\pm 0.4\%$	n/a
		heavy flavor (b, c)	-1.9/+2.9%	-3.5/+2.5%	n/a
		$t\bar{t}$	-0.9/+0.8%	$\pm 1.0\%$	$\pm 3.3\%$
		QCD, muon	$\pm 0.8\%$	$\pm 1.7\%$	$\pm 0.9\%$
		QCD, electron	$\pm 0.4\%$	$\pm 0.8\%$	-0.4/+0.3%
		s-, tW ch., dibosons, Z+jets	$\pm 0.3\%$	$\pm 0.6\%$	$\pm 0.5\%$
		Total marginalised uncertainty	-7.7/+7.9%	-7.7/+7.8%	n/a
		Luminosity		$\pm 2.2\%$	
		Total			
Not marginalised	Theor. uncert.	Scale, $t\bar{t}$	-3.3/+1.0%	$\pm 0.9\%$	-4.0/+2.1%
		Scale, W+jets	-2.8/+0.3%	-0.0/+3.4%	n/a
		Scale, $t$ , $s$ , tW channels	-0.4/+1.0%	$\pm 0.2\%$	-2.2/+2.3%
		Matching, $t\bar{t}$	$\pm 1.3\%$	$\pm 0.4\%$	$\pm 0.4\%$
		$t$ -channel generator	$\pm 4.2\%$	$\pm 4.6\%$	$\pm 2.5\%$
		PDF	$\pm 1.3\%$	$\pm 1.3\%$	$\pm 2.5\%$
		Total theor. uncertainty	-6.3/+4.8%	-4.9/+5.9%	-5.6/+4.9%
		Syst. + theor. + luminosity uncert.	-8.1/+7.8%	-8.1/+8.4%	$\pm 10.8\%$
		Total (stat. + syst. + theor. + lum.)	-10.1/+9.5%	-9.4/+10.0%	$\pm 13.8\%$
		Total			